

## THE SEARCH FOR SUPER-SATURATION IN CHROMOSPHERIC EMISSION

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Received 2010 October 11; accepted 2011 June 22; published 2011 August 22

### ABSTRACT

We investigate if the super-saturation phenomenon observed at X-ray wavelengths for the corona exists in the chromosphere for rapidly rotating late-type stars. Moderate resolution optical spectra of fast-rotating EUV- and X-ray-selected late-type stars were obtained. Stars in  $\alpha$  Per were observed in the northern hemisphere with the Isaac Newton 2.5 m telescope and Intermediate Dispersion Spectrograph. Selected objects from IC 2391 and IC 2602 were observed in the southern hemisphere with the Blanco 4 m telescope and R-C spectrograph at CTIO. Ca II H and K fluxes were measured for all stars in our sample. We find the saturation level for Ca II K at  $\log(L_{\text{CaK}}/L_{\text{bol}}) = -4.08$ . The Ca II K flux does not show a decrease as a function of increased rotational velocity or smaller Rossby number as observed in the X-ray. This lack of “super-saturation” supports the idea of coronal stripping as the cause of saturation and super-saturation in stellar chromospheres and coronae, but the detailed underlying mechanism is still under investigation.

**Key words:** open clusters and associations: individual ( $\alpha$  Per, IC 2391, IC 2602) – stars: activity – stars: chromospheres – stars: late-type – stars: rotation

### 1. INTRODUCTION

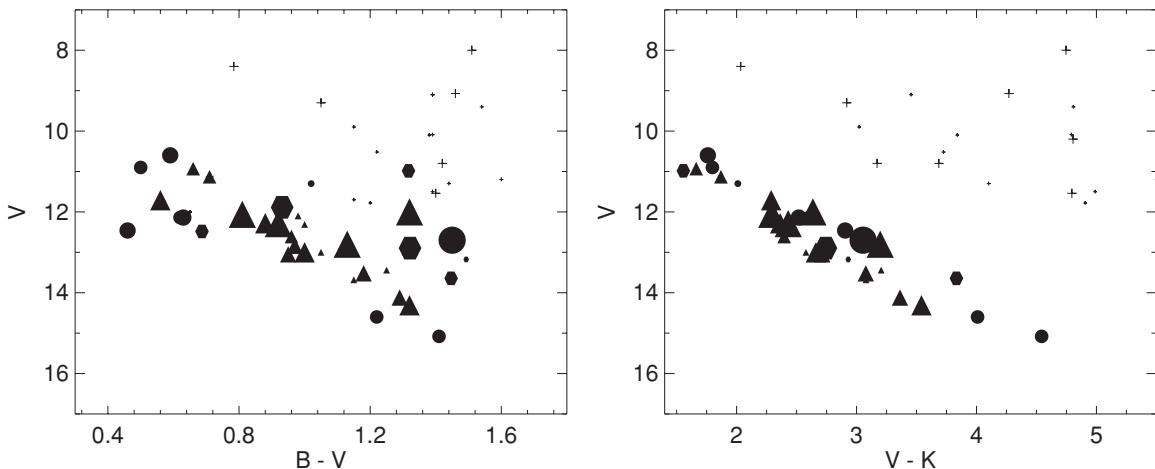
The Sun’s chromosphere is a complex region where pressure dominance at the lower photosphere becomes magnetic dominance at high altitudes in the atmosphere. Energy dissipation in the chromosphere and the associated heating processes have been a topic of intense debate. Virtually all late-type stars with surface convective envelopes (types F to M) have chromospheres and it has been well established that the strength of the dynamo action increases with stellar rotation rates (Skumanich 1972). A better understanding of the Sun’s outer atmosphere can help us to understand other stars while stars of different age and mass can provide a better understanding of the evolution of the solar dynamo.

In recent years, much observational effort has concentrated on the study of open clusters (Soderblom 1998; Jeffries 1999). In the younger clusters ( $\alpha$  Per, 50 Myr) a large number of G and K dwarfs are rotating rapidly ( $v \sin i \geq 100 \text{ km s}^{-1}$ ), whereas in the older Hyades and in the solar neighborhood rapid rotation is confined to the M dwarfs. When comparing the activity properties of stars covering a large range of masses, the Rossby number  $N_R$  (ratio of rotation period to convective turnover time  $\tau_c$ ) has often been used instead of the rotational period (Simon & Fekel 1987; Mathioudakis et al. 1995). This is because, in addition to the dynamo’s dependence on rotation, there is an increase in the convective turnover time for lower mass stars (Kim & Demarque 1996).

The Rossby diagram for open clusters has shown that the “plateau” of coronal saturation occurs for  $L_X/L_{\text{bol}} \approx 10^{-3}$  to  $10^{-4}$  (Stauffer et al. 1997; Queloz et al. 1998; Pizzolato et al. 2003). Saturation can be understood in terms of the limited area of the stellar surface. As more surface field is generated with increased rotation and deep convection, a point is eventually reached where the stellar surface is totally covered with active regions. The footpoints of magnetic loops crowd each other out and no more new loops can be generated. Consequently, the heating reaches a maximum and so does the radiative emission. In that scenario, the emission would be expected

to scale with surface area. A second explanation for the saturation is based on the feedback between the induced fields and velocities in the convection zone. As an increased angular velocity generates stronger magnetic fields, a point is eventually reached where the ratio between the total magnetic energy and kinetic energy approaches unity. The equipartition achieved provides an upper boundary to the total magnetic energy, since the Lorentz forces ( $\mathbf{J} \times \mathbf{B}$ , the vector cross product of the current density  $\mathbf{J}$  and magnetic field  $\mathbf{B}$ ) suppress convection. These strong Lorentz forces help in reducing differential rotation and therefore its ability to induce toroidal field from the poloidal. As a result limited atmospheric emission will be created and is expected to be a function of parameters such as the stellar radius (Glatzmaier 1985). In general chromospheric saturation has been found to occur at similar Rossby numbers as coronal saturation (Marsden et al. 2009) and saturation of the coronal emission has been interpreted as saturation of the dynamo itself (Vilhu & Walter 1987). However, Mathioudakis et al. (1995) found some evidence for coronal saturation to occur at lower Rossby numbers (higher rotation rates) than chromospheric saturation. Reiners et al. (2009) find that saturation of the magnetic flux can occur at lower rotational velocities for M dwarfs and understanding saturation in these different regimes remains a challenge to both observations and theories.

Several extremely fast rotators have been observed to show a decline in their coronal emission with increasing rotation. This effect has been termed *super-saturation* (Prosser et al. 1996; Stauffer et al. 1997; Queloz et al. 1998; James et al. 2000). One explanation for this effect has been given as resulting from the reduction of the X-ray emitting volume of rapid rotators by centrifugal stripping (Jardine 2004). The increased rotational velocity will decrease the apparent surface gravity and cause increased pressure in the outer parts of large coronal loops. The magnetic field lines get distorted and eventually break open leading to saturation. Combined with a saturated dynamo these processes will ultimately lead to a reduction in the coronal X-ray emission. Recently, Jeffries et al. (2011) have shown support for the centrifugal stripping idea for explaining



**Figure 1.** Color-magnitude diagrams for our sample of stars. Shown in the left panel is  $V$  magnitude vs.  $B - V$ , and  $V$  vs.  $V - K$  is shown in the right panel. Stars from  $\alpha$  Per are shown as triangles, the southern clusters IC2391 and IC2602 are shown as circles and hexagons, respectively, and miscellaneous solar neighborhood stars are shown as crosses. Symbol sizes are proportional to rotational velocities, with the smallest symbols shown for  $v \sin i < 25 \text{ km s}^{-1}$  and the largest for  $v \sin i > 150 \text{ km s}^{-1}$ .

super-saturation using *XMM-Newton* observations of K and M stars in NGC 2547. Thus for super-saturated stars, the hot coronal plasma will become unstable and cool down to chromospheric temperatures (Antiochos et al. 1986; Stern 1999). More cool loops emitting in chromospheric and transition region lines can exist but not in X-rays. This would imply that there should be no evidence for super-saturation at chromospheric temperatures.

Recent work has supported this expected lack of super-saturation in the chromosphere. Observing the Ca IR triplet, Marsden et al. (2009) found no evidence for super-saturation in the chromosphere for young open clusters IC 2391 and IC 2602. Such studies were extended to rapidly rotating M dwarfs in NGC 2516 (Jackson & Jeffries 2010), which also found no decrease in chromospheric emission even at very low Rossby numbers ( $\lesssim 0.01$ ).

The present paper uses moderate resolution spectra for a sample of fast-rotating late-type stars to search for the effects of super-saturation in their chromospheres. A description of the sample selection criteria is given in Section 2.1. In Section 2.2 we describe the observations, instrumental setup, and data reduction techniques. In Section 3 we present our results including measurements of the chromospheric emission in terms of Ca II K and make a comparison with the rotational velocities and Rossby numbers, and in Section 4 we discuss trends for these parameters and compare the results to super-saturation models for the chromosphere. Lastly, in Section 5 we summarize our findings.

## 2. OBSERVATIONS AND DATA REDUCTION

### 2.1. Sample Selection

Our samples consist of 72 active late-type stars with projected equatorial rotation velocities in the range  $20\text{--}200 \text{ km s}^{-1}$ . Our northern sample concentrated on stars in  $\alpha$  Per (Randich et al. 1996) while our southern sample includes stars from IC 2391 (Patten & Simon 1996; Stauffer et al. 1997) and IC 2602 (Randich et al. 1995; Stauffer et al. 1997). The optical identification campaigns that followed X-ray and EUV surveys provided some additional solar neighborhood targets (Jeffries et al. 1998; Christian et al. 2001; Christian & Mathioudakis 2002; Hüensch et al. 2004).  $V$  magnitude versus the color index,

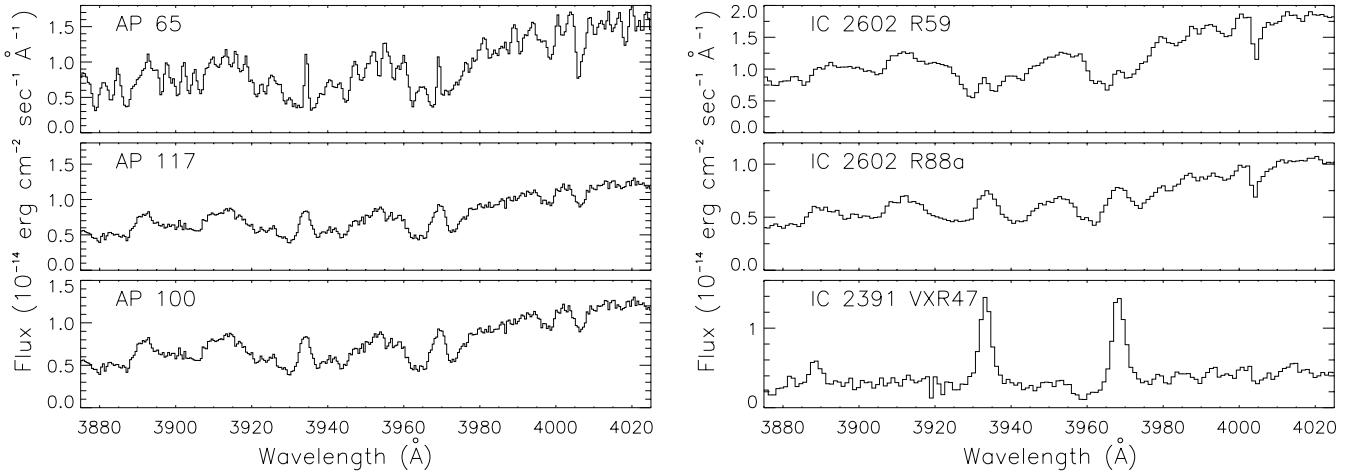
$B - V$ , is shown for our sample in Figure 1 (left panel), and  $V - K$  computed from  $K$  colors from the Two Micron All Sky Survey catalog is shown in Figure 1 (right panel). The reduced scatter demonstrates that  $V - K$  is a more suitable color for these late spectral types.

### 2.2. Optical Observations and Analysis

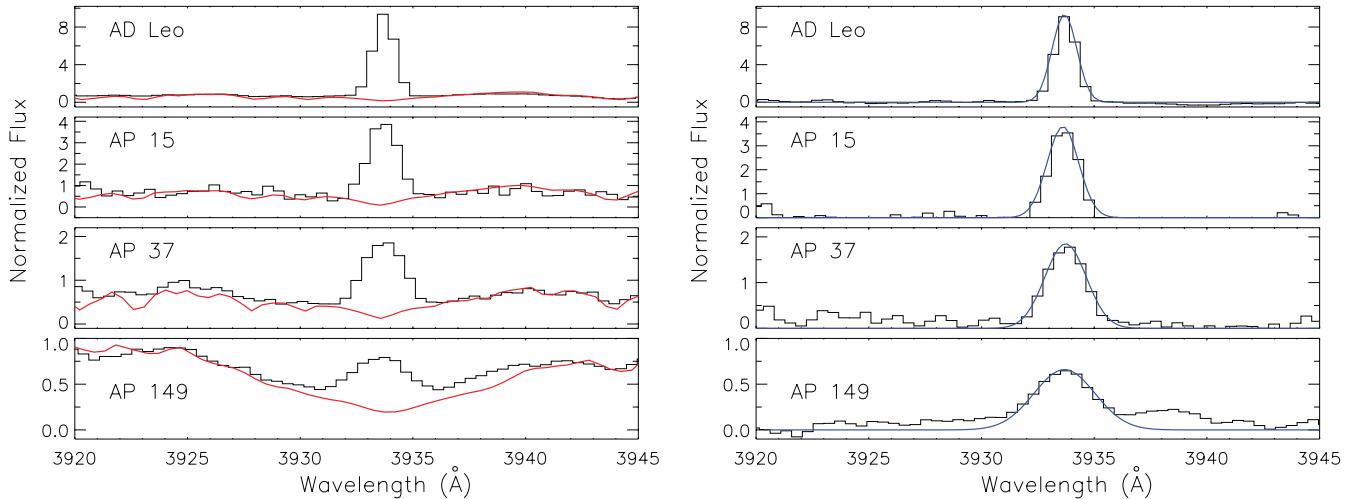
The southern objects were observed using the CTIO Blanco 4 m telescope and R-C spectrograph, while in the north we used the 2.5 m Isaac Newton Telescope (INT) equipped with the Intermediate Dispersion Spectrograph (IDS). The CTIO observations were obtained on two nights in 2005 February 23–24. The KPGL1 grating was used, giving a resolution of  $1 \text{ \AA pixel}^{-1}$  and covering the range  $\approx 3300\text{--}5800 \text{ \AA}$ . Spectra were bias subtracted and flat fielded with an internal quartz lamp, and the wavelength calibration was established with HeNeAr lamps. The INT spectra were obtained on 2007 December 23–27 using the R1200B grating. Our setup covered the  $3600\text{--}4600 \text{ \AA}$  range with a spectral resolution of  $0.47 \text{ \AA pixel}^{-1}$ . Wavelength calibration was established using CuAr plus CuNe lamps before and after each exposure. Flat fields were obtained with a quartz lamp. Several radial velocity standards and flux standards were used to establish the accuracy of the velocity scale and flux calibration, respectively. The observations were reduced using standard routines within IRAF. Two-dimensional images were bias subtracted and flat fielded with the *ccdred* package and wavelength and flux calibrated with the *refspec* and *calibrate* routines within *noao.onedspec*, respectively.

The Ca II H and K line fluxes were derived by fitting Gaussians to the flux calibrated spectra as described below. We focus on the Ca II K line at  $\lambda\lambda 3933$  due to the possible blending of Ca II H with He. We show a sample of sources with both strong Ca II H and K in emission in Figure 2.

To estimate the photospheric contribution to the Ca II line fluxes we constructed stellar models using the Spectroscopy Made Easy (SME) code (Valenti & Piskunov 1996). Models were created from 3500 to 6500 K in 300 K steps for solar metallicities and gravity  $\log g = 4.5$ . Additional models were created at each temperature for appropriate values of  $v \sin i$  from 0 to  $200 \text{ km s}^{-1}$ . The normalization and the systemic radial velocity  $v_{\text{rad}}$  were left as free parameters. Atomic line data were obtained from the Vienna Atomic Line Database (Piskunov et al. 1995).



**Figure 2.** Sample Ca II H and K spectra. The left panel shows sample INT IDS spectra for: AP 65, a K star with rotational velocity of  $10 \text{ km s}^{-1}$ , AP 117, a K star with a rotational velocity of  $83 \text{ km s}^{-1}$ , and AP 100, an ultrafast-rotating K7 star with  $v \sin i = 205 \text{ km s}^{-1}$ . Shown in the right panel are sample spectra taken with the R-C spectrograph at CTIO for: IC 2602 R59, a K0 star with a rotational velocity of  $34 \text{ km s}^{-1}$ , IC 2602 R88a, an ultrafast-rotating K4 star with  $v \sin i = 200 \text{ km s}^{-1}$ , and IC 2391 VXR 47, a fast-rotating M star with  $v \sin i = 95 \text{ km s}^{-1}$ .



**Figure 3.** Sample spectra including a synthesized photospheric model from SME. The left panel shows the observed spectra plotted as the black histogram and the SME model is overplotted as the solid red line. The right panel shows the difference between the observed spectrum and SME model overplotted with the fitted Gaussian as a solid blue line. Shown from top to bottom in both panels are: AD Leo ( $T = 3600 \text{ K}$ ,  $v \sin i = 6 \text{ km s}^{-1}$ ), AP 15 ( $T = 4000 \text{ K}$ ,  $v \sin i = 52 \text{ km s}^{-1}$ ), AP 37 ( $T = 4900 \text{ K}$ ,  $v \sin i = 29 \text{ km s}^{-1}$ ), and AP 149 ( $T = 6300 \text{ K}$ ,  $v \sin i = 117 \text{ km s}^{-1}$ ).

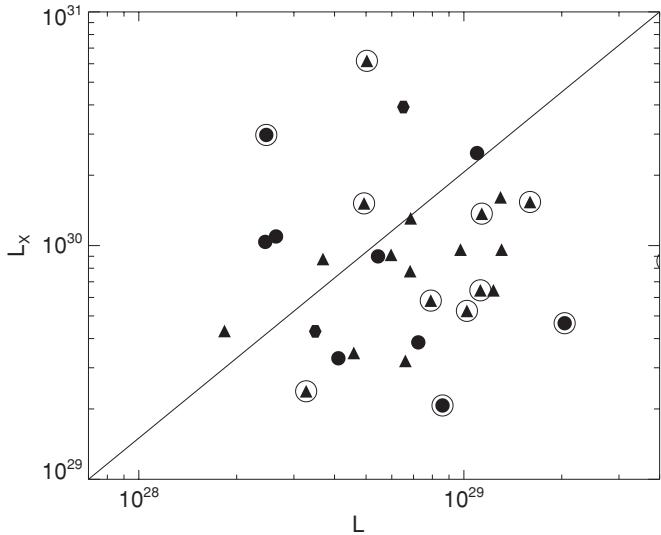
The SME models were then subtracted from each observed spectrum using the model closest in temperature ( $T$ ) and  $v \sin i$ . The differences between the observed (chromospheric) contribution and SME model (photospheric) contribution were then re-fitted with a new Gaussian. Spectra for representative stars at four different temperatures are shown in Figure 3. In general we find the photosphere contribution is about 50%. However, photospheric contributions for the latest spectral types ( $T < 4000 \text{ K}$ ) are in general smaller and on the order of 10%. Typical photospheric contributions in the temperature range between 4000 and 5500 K are  $\approx 50\%$ , but can be as high as a factor of  $\approx 2\text{--}3$  for stars with temperatures above 5500 K and for those with the weakest emission. In general the photospheric contribution will depend not only on a star's temperature, but its chromospheric activity level and rate of rotation. We note any photospheric contribution not accounted for will only act to increase the Ca fluxes, not decrease them.

Surface fluxes are calculated using the relationship between observed flux and surface flux given in Oranje et al. (1982), Rutten et al. (1989), Mathioudakis & Doyle (1989), and Mathioudakis & Doyle (1992). Reddening values for  $\alpha$  Per were

taken from Randich et al. (1996) with  $E(B - V) = 0.1$ , and from Patten & Simon (1996) for IC 2391 and Randich et al. (1995) for IC 2602 with  $E(B - V) = 0.006$  and  $0.04$ , respectively. Bolometric corrections were taken from Johnson (1966) and Bessell (1991). Rotational velocities ( $v \sin i$ ) were taken from the literature, and rotational periods,  $P$ , were derived from these using  $P = 2\pi R_*/v \sin i$ , where  $R_*$  is the stellar radius from the ratio of the stellar flux to observed flux as given in Equation (1) in Mathioudakis & Doyle (1992). Possible sources of error in the periods from the stellar radii are treated in Section 3. Marsden et al. (2009) have shown rotational velocity values for IC 2391 and IC 2602 from the literature to be in good agreement with their derived values.

Previously (Christian & Mathioudakis 2002) we had used relations for Rossby number and  $B - V$  from Noyes et al. (1984). However these relations are flat for later-type stars with  $B - V > 1$  (see the discussion in Jeffries et al. 2011), and we calculated the Rossby number using the relation:

$$\log(N_R) = \log(P) - 1.1 + 0.5 \log(L_{\text{bol}}/L_{\odot}) \quad (1)$$



**Figure 4.** X-ray luminosity  $L_X$  plotted as a function of Ca K luminosities  $L_{\text{CaK}}$  for cluster member stars. Stars showing super-saturation from James et al. (2000) are also indicated with an open circle. This shows a slight trend indicating that stars with super-saturation in the X-rays have higher chromospheric emission (see the text). Stars from  $\alpha$  Per are shown as triangles; the southern clusters IC2391 and IC2602 are shown as circles and hexagons, respectively.

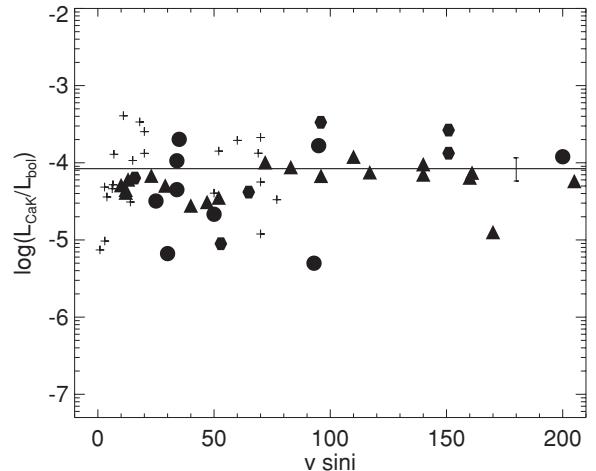
from Jeffries et al. (2011). Here,  $N_R$  is the Rossby number,  $P$  is the stellar rotation period,  $L_{\text{bol}}$  is the bolometric luminosity, and  $L_\odot$  is the solar bolometric luminosity. The scale factor 1.1 is set for the log of the convective turnover time for solar-type stars (Noyes et al. 1984; Jeffries et al. 2011).

### 3. RESULTS

Approximately 85% of the stars in our sample showed Ca II H and K in emission. The remaining 15% had no detectable Ca II H and K in emission. These objects are of the earlier spectral types,  $B - V < 0.6$ , and the non-detection is most likely due to the combination of strong photospheric continuum and spectral resolution rather than the absence of a chromosphere. The Ca II H and K line fluxes and stellar parameters are shown in Table 1. We computed the  $L_{\text{CaK}}/L_{\text{bol}}$  for the stars in our sample using the relationship between observed flux and surface flux (Rutten et al. 1989; Mathioudakis & Doyle 1989).

The X-ray emission of coronally active late-type stars saturates at  $\approx 1$  part in 1000 of the star's bolometric luminosity ( $L_X/L_{\text{bol}}$ ). Many stars in our sample have  $L_X/L_{\text{bol}}$  between  $10^{-3}$  and  $10^{-4}$ . We compare the X-ray and Ca II K luminosity ratios in Figure 4. In the figure we have indicated stars showing super-saturation in X-rays from James et al. (2000) ( $L_X/L_{\text{bol}}$  and  $v \sin i > 90 \text{ km s}^{-1}$ ), and the figure shows a slight trend that stars with higher chromospheric luminosity have lower X-ray luminosities. The  $L_{\text{CaK}}$  luminosities for the super-saturated stars differ from the entire sample with a modest, but significant Kolmogorov–Smirnov statistic of 0.6.

In Figure 5 we plot the  $L_{\text{CaK}}/L_{\text{bol}}$  as a function of  $v \sin i$ . The average  $\log(L_{\text{CaK}}/L_{\text{bol}})$  is  $-4.08$ . We have estimated the errors for  $\log(L_{\text{CaK}}/L_{\text{bol}})$  combining a 10% uncertainty in the flux estimates and an additional 10% possible systematic error in converting from counts to flux along with any uncertainty in radii used in calculating the bolometric luminosities (generally less than 10%). Combining these errors, we conservatively estimate a 30% uncertainty in  $L_{\text{CaK}}/L_{\text{bol}}$  and show a sample error of 30% in Figure 5. Although there is significant scatter below



**Figure 5.** Ca II K luminosities normalized to the bolometric luminosity as a function of rotational velocity. Symbols are the same as Figure 3, with the inclusion of the miscellaneous solar neighborhood stars shown as crosses. A line is shown for the mean  $L_{\text{CaK}}/L_{\text{bol}}$  and a sample error bar is shown at  $v \sin i = 180 \text{ km s}^{-1}$ .

$50 \text{ km s}^{-1}$ , there is no evidence for a decrease in  $L_{\text{CaK}}/L_{\text{bol}}$  for the highest rotational velocities and this is treated in Section 4. The low point in the figure, at  $\approx 170 \text{ km s}^{-1}$ , is AP 139, which had an anomalously low Ca II K flux for its rotational velocity; however, its rotational velocity was determined from its photometric period (Stauffer et al. 1997), and it may actually be a binary.

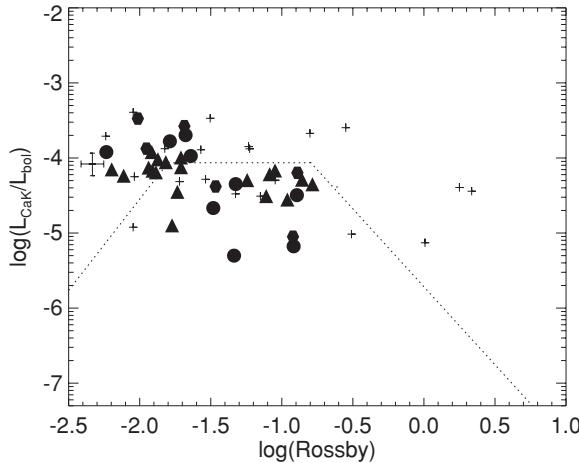
To compare the rotation and activity of our sample of stars with different masses and radii it is convenient to use the Rossby number  $N_R$  (ratio of rotation period to convective turnover time  $\tau_c$ ) (Jeffries et al. 2011). Periods were derived from rotational velocities and stellar radii calculated from Mathioudakis & Doyle (1992) as described in Section 2.2. A 20% error in the stellar radii will cause a 20% error in derived periods, but this only translates to a change in  $\log(N_R)$  of 0.08. The saturation levels of coronal X-rays are reached at  $\log(N_R) \approx -1$  ( $L_X/L_{\text{bol}} \approx 10^{-3}$ ) and extend to  $\log(N_R) \approx -1.8$  (Jeffries et al. 2011). Similar ranges were found for pre-main-sequence stars by Feigelson et al. (2003). The discovery of super-saturation at the highest stellar rotation rates (Prosser et al. 1996; Randich et al. 1996; Stauffer et al. 1997) was recently confirmed using a sample of G and K dwarfs by Jeffries et al. (2011). The same authors do not find strong evidence for super-saturation in M dwarfs. Some evidence for super-saturation has also been found in the extreme ultraviolet (Christian & Mathioudakis 2002).

Our sample has 26 stars with the log of the Rossby number,  $\log(N_R)$ , less than  $-1.6$ . In Figure 6, we plot our Ca II K luminosities ( $L_{\text{CaK}}/L_{\text{bol}}$ ) as a function of Rossby number. Although there is a large amount of scatter in  $L_{\text{CaK}}/L_{\text{bol}}$  for the lowest Rossby numbers, there is no obvious decrease in  $L_{\text{CaK}}/L_{\text{bol}}$  for the fastest rotators ( $\log(N_R) < -1.8$ ). We overplot (dotted line) linear fits to the X-ray observations from Jeffries et al. (2011) in the three regimes:  $\log(N_R) < -1.8$ ,  $-1.8 < \log(N_R) < -0.8$ , and  $\log(N_R) > -0.8$ , where we used the slopes in these regions and set the saturated region to the mean of  $L_{\text{CaK}}/L_{\text{bol}}$ . We note that the overplotted loci are not formally correct for the latest-type stars in our sample, but they are included for comparison. We have converted the published rotational velocities to periods for calculations of the Rossby numbers and this may add some additional uncertainty, but in the  $x$ -direction, not in  $L_{\text{CaK}}/L_{\text{bol}}$ . We show a sample error of

**Table 1**  
Ca H and K Line Fluxes and Stellar Parameters

Source <sup>a</sup>	Line Fluxes <sup>b</sup>		<i>d</i>	<i>mv</i>	<i>B</i> – <i>V</i>	<i>V</i> – <i>K</i>	<i>v</i> sin <i>i</i>	log( <i>L</i> <sub>CaK</sub> / <i>L</i> <sub>bol</sub> ) <sup>b</sup>	log( <i>L</i> <sub>X</sub> / <i>L</i> <sub>bol</sub> ) <sup>c</sup>	<i>N<sub>R</sub></i> <sup>d</sup>	Comment <sup>e</sup>
	Ca K (10 <sup>–14</sup> erg cm <sup>–2</sup> s <sup>–1</sup> Å <sup>–1</sup> )	Ca H (10 <sup>–14</sup> erg cm <sup>–2</sup> s <sup>–1</sup> Å <sup>–1</sup> )									
VXR60n	5.2	5.9	160.0	13.0	1.31	2.71	150	–3.90	–3.52	–1.97	IC 2391
VXR60s	3.5	2.7	160.0	13.2	1.49	2.92	15	–4.23	–3.44	–0.90	S97
VXR47	5.0	4.9	160.0	13.7	1.44	3.81	95	–3.50	–3.36	–2.03	S97
R50a	1.1	0.5	160.0	12.5	0.68	–0.96	64	–4.41	–3.32	–1.47	S97
R62a	2.1	2.2	160.0	11.0	1.31	1.54	52	–5.08	...	–0.94	S97
R80a	13.6	11.8	160.0	12.0	0.92	–1.79	150	–3.60	–3.29	–1.70	S97
R3	3.6	1.0	160.0	11.3	1.02	2.01	25	–4.50	–3.14	–0.89	IC 2602
R24a	1.3	2.1	160.0	14.6	1.22	4.01	34	–3.97	–3.07	–1.64	S97
R31	2.4	2.1	160.0	15.1	1.41	4.54	35	–3.70	–2.97	–1.68	S97
R43	0.9	0.4	160.0	12.1	0.63	2.52	50	–4.67	–3.05	–1.48	S97
R52	6.7	5.7	160.0	12.5	0.46	2.90	95	–3.78	–3.42	–1.79	S97
R58	0.8	...	160.0	10.6	0.59	1.76	93	–5.30	–3.22	–1.34	S97
R59	1.8	1.5	160.0	12.1	0.62	2.60	34	–4.35	–3.13	–1.32	S97
R83	0.8	0.2	160.0	10.9	0.50	1.80	30	–5.18	–3.55	–0.92	S97
R88a	2.8	2.9	160.0	12.7	1.45	3.05	200	–3.92	–3.54	–2.23	S97
J1131–34.6	39.4	45.3	18.0	11.5	1.40	4.80	60	–3.71	–3.34	–2.24	EUV
J0825–16.3	44.8	53.4	46.0	10.5	1.22	3.72	20	–3.88	–3.12	–1.23	EUV
J1258–70.4	11.7	9.0	330.0	12.0	0.65	–3.08	20	–3.60	–3.40	–0.55	EUV
HD 174429	290.3	162.8	160.0	8.4	0.78	2.03	70	–3.67	...	–0.80	
GJ 431	68.2	80.8	29.0	11.5	1.39	4.99	18	–3.47	–3.01	–1.50	
AP 15	0.5	0.5	176.0	14.1	1.29	3.36	52	–4.45	–3.08	–1.73	α Per, R96
AP 25	1.9	1.3	176.0	12.2	0.88	2.24	12	–4.35	–3.07	–0.78	
AP 37	1.6	1.0	176.0	12.6	0.96	2.40	29	–4.29	–3.11	–1.24	R96
AP 43	2.6	2.7	176.0	12.8	0.97	2.73	72	–3.99	–3.00	–1.71	R96
AP 56	2.8	2.6	176.0	13.0	1.00	2.66	110	–3.92	–3.21	–1.91	R96
AP 63	3.0	2.7	176.0	12.3	0.92	2.43	161	–4.13	–3.37	–1.94	R96
AP 65	1.2	0.9	176.0	13.0	1.05	2.58	10	–4.29	–3.41	–0.86	R96
AP 86	0.9	1.0	176.0	14.3	1.32	3.54	140	–4.15	–3.29	–2.20	R96
AP 95	3.9	2.4	176.0	12.3	0.88	2.36	140	–4.02	<–3.29	–1.87	R96
AP 100	2.1	1.7	176.0	12.8	1.13	3.20	205	–4.24	–3.37	–2.11	R96
AP 112	1.0	0.9	176.0	13.7	1.15	3.08	13	–4.22	–2.84	–1.09	R96
AP 124	1.3	1.4	176.0	13.4	1.25	3.20	...	–4.18	<–3.36	...	R96
AP 117	1.8	1.8	176.0	13.1	0.95	2.71	83	–4.06	–3.00	–1.82	R96
AP 118	3.1	1.7	176.0	12.1	0.81	2.29	160	–4.19	–3.11	–1.89	R96
AP 139	1.3	0.5	176.0	12.0	1.32	2.64	170	–4.90	–3.41	–1.77	R96
AP 149	4.3	2.8	176.0	11.7	0.56	2.29	117	–4.12	–3.14	–1.71	R96
AP 167	1.4	1.4	176.0	13.5	1.18	3.08	96	–4.17	–2.08	–1.91	R96
AP 197	1.8	1.3	176.0	12.3	1.00	–3.01	12	–4.39	–3.70	–0.62	R96
AP 199	3.5	2.4	176.0	12.1	0.98	2.51	23	–4.17	–3.30	–1.05	R96
HE 350	3.3	2.1	176.0	11.1	0.71	1.87	47	–4.51	–3.79	–1.11	R96
HE 917	3.5	2.3	176.0	10.9	0.66	1.66	40	–4.55	–3.46	–0.96	R96
HD 19305 <sup>f</sup>	13.7	10.0	14.8	9.1	1.39	3.45	0	–5.13	...	0.01	
HD 17878	0.7	1.0	74.0	3.9	0.73	–4.49	25	–8.10	...	1.41	
HD 283518	10.7	11.1	136.8	10.8	–1.02	3.17	77	–4.48	...	–1.33	
HD 283571	39.9	18.4	133.5	10.2	0.90	4.80	52	–3.95	...	–1.23	
V1005 Ori	22.1	20.9	26.7	10.1	1.38	3.84	14	–4.51	...	–1.15	
J0723+20	26.9	33.2	25.8	9.9	1.15	3.02	10	–4.30	...	–1.05	RE
YZ CMi	25.9	30.5	5.9	11.2	1.60	5.50	6	–4.28	...	–1.54	
REJ0808+21	17.0	11.3	6.0	11.7	1.15	5.62	...	–3.78	...	...	RE
CV Cnc	1.9	1.9	12.8	13.6	1.50	5.88	6	–4.48	...	...	
J1004+50	31.0	34.3	14.0	11.3	1.44	4.10	15	–3.97	...	–1.67	EUV
GJ 380	173.6	130.2	4.9	6.6	1.38	3.64	3	–5.01	...	–0.51	
AD Leo	103.1	92.7	4.7	9.4	1.54	4.81	6	–4.34	–3.21	–1.31	
CN Leo	5.0	4.8	2.3	13.5	2.01	7.42	2	–4.32	...	–1.72	
GJ 411	302.0	136.0	2.5	8.0	1.51	4.75	50	–4.39	–4.30	0.25	
HD 131156	1624.0	950.0	25.0	4.6	0.77	2.63	3	–4.44	...	0.34	
J2131+23	96.7	93.9	25.1	9.3	1.05	2.92	69	–3.93	...	–1.82	EUV
EV Lac	95.3	127.3	5.1	10.1	1.39	4.79	6	–3.89	...	–1.57	
FK Aqr	35.2	35.9	8.6	9.1	1.46	4.27	70	–4.92	...	–2.05	
GT Peg	10.5	10.4	14.3	11.8	1.20	4.91	11	–3.39	...	–2.05	
GJ 890	24.2	31.1	22.0	10.8	1.42	3.69	70	–4.25	–3.18	–2.04	

**Notes.**<sup>a</sup> Star names using the convention of Stauffer et al. (1997) for IC2391 and IC 2602, and Randich et al. (1996) for α Per.<sup>b</sup> Ca H and Ca K fluxes and *L*<sub>CaK</sub>/*L*<sub>bol</sub> from the current work.<sup>c</sup> X-ray luminosity, *L*<sub>X</sub>/*L*<sub>bol</sub>, and *v* sin *i* references with S97 = Stauffer et al. (1997) for IC 2391 and IC 2602, unless otherwise noted. R96 = Randich et al. (1996) for α Per (AP); J00 = James et al. (2000).<sup>d</sup> *N<sub>R</sub>*, Rossby number (Jeffries et al. 2011).<sup>e</sup> Comment of Star Cluster Name or abbreviated star name; RE for ROSAT EUV and EUVE for *Extreme Ultraviolet Explorer* from Christian & Mathioudakis (2002).<sup>f</sup> Start of solar neighborhood stars.



**Figure 6.** Ca K luminosities normalized to the bolometric luminosity shown as a function of Rossby number  $N_R$  for all stars from our sample. Overplotted are the luminosity levels and ranges from Jeffries et al. (2011) fitted to the median  $L_{\text{CaK}}/L_{\text{bol}}$  showing saturation of the X-rays and their decline at smallest Rossby numbers (see the text). Symbols are the same as Figure 1, and a sample error bar is shown at  $\log(N_R) \approx -2.3$  for  $L_{\text{CaK}}/L_{\text{bol}}$  and  $\log(N_R)$ .

$\log(N_R) \approx 0.08$  in Figure 6. For example, using the Rossby relation from Noyes et al. (1984) generally finds values 0.2 higher than the Jeffries et al. (2011) relation shown in Figure 6, but the Noyes et al. (1984) relation is not correct for stars with  $B - V > 1$ , as discussed in Section 2.2.

#### 4. DISCUSSION: $L_{\text{CaK}}/L_{\text{bol}}$ AND CHROMOSPHERIC EMISSION

Marsden et al. (2009) found saturation to set in near  $\log(N_R) = -0.8$  using observations of the Ca II IR triplet for the fast rotators in IC 2391 and IC 2602. Although our Rossby diagram (Figure 6) has much scatter, we find a saturation level for the Ca K emission at  $\log(L_{\text{CaK}}/L_{\text{bol}})$  of  $-4.08$  and to be consistent with saturation setting in at  $\log(N_R)$  of  $\approx -0.8$ , although given the limited sample and scatter, the range could be between  $\log(N_R) \approx -0.6$  and  $-1.0$ .

The coronal emission of very fast rotating stars begins to decrease at a  $v \sin i > 100 \text{ km s}^{-1}$  and a Rossby number of  $\approx -1.6$ . Several authors (Stauffer et al. 1997; Queloz et al. 1998; James et al. 2000) have observed that coronal emission decreased for the fastest rotating stars ( $v \sin i > 100 \text{ km s}^{-1}$ ) and at a Rossby number of  $\approx -1.6$ . No significant decrease of  $L_{\text{CaK}}/L_{\text{bol}}$  with higher rotational velocities or lower Rossby numbers was observed in our sample. The mean  $L_{\text{CaK}}/L_{\text{bol}}$  was  $8.76 \times 10^{-5}$  for stars with  $v \sin i < 100 \text{ km s}^{-1}$  and the average for stars with  $v \sin i > 100 \text{ km s}^{-1}$  was  $9.68 \times 10^{-5}$ . These two values differ by  $\approx 10\%$  and are well within uncertainties. For comparison, the X-ray sample of K and M stars shows a decrease of the mean  $\log(L_X/L_{\text{bol}})$  from  $-3.0$  for the complete sample to  $-3.5$  for stars at  $\log(N_R) \lesssim -2$  (Jeffries et al. 2011). Marsden et al. (2009) find a similar decrease for the X-ray saturation levels for the fastest rotators. However, here we have found no evidence for the decrease in the chromospheric emission of Ca II K.

Marsden et al. (2009) suggest that saturation in the chromosphere (8542 Å) and corona occur at a Rossby number of  $\approx -1$ . The Mg II results from Cardini & Cassatella (2007) suggest that saturation occurs at  $\log(N_R) \approx -0.7$ . However, Marsden et al. (2009) argue these are possibly still within the error bars. Also, the results of Feigelson et al. (2003) and James et al. (2000) find

that the saturation levels for the corona may occur as early as a Rossby value of  $-0.7$ . Although we agree these results may be within the errors for saturation at Rossby values of  $-1$  seen for the corona, we can then ask: what does this mean if the corona actually reaches saturation at a higher Rossby number (slower rotation rate) than the chromosphere? This may be related to the fact that the co-rotation radius is larger for slower rotators and the onset of saturation of the dynamo can occur at higher Rossby number in both the corona and chromosphere, although the exact mechanism for saturation is presently not well understood.

An explanation for the saturation of coronal X-rays has been given as the reduction of the X-ray emitting volume of late-type stars due to centrifugal stripping (James et al. 2000; Jardine & Unruh 1999; Marsden et al. 2009). The increased rotational velocity decreases the apparent surface gravity and the centrifugal forces increase the pressure and density in the loop summits. This outward pressure may eventually force the largest closed loops to open up, releasing their plasma into the stellar wind. This process would reduce the volume of confined plasma in the corona and would therefore reduce the overall X-ray emission, potentially masking the onset of dynamo saturation. Support for the coronal stripping model has been found by Jardine (2004).

An additional effect of rapid rotation has also been suggested by Antiochos et al. (1986) and Stern (1999). Since at any given height the plasma pressure decreases with decreasing temperature, low-temperature loops have a lower pressure than high-temperature loops and are therefore less susceptible to centrifugal stripping. If rapid rotators were to possess a higher proportion of cool loops, these could remain closed out to heights where hotter loops would have been opened up by their internal pressure. These cool loops might contribute to the UV and EUV radiation, but not to X-rays. The shape of the emission measure distribution with temperature would therefore shift, with more emission appearing at lower temperatures. Thus, if the coronal heating mechanism in rapid rotators were to favor the production of a greater fraction of cool loops than in slowly rotating stars, this might explain the saturation of the X-ray emission measure with increasing rotation rate. This would also imply that there should be no evidence for super-saturation at chromospheric temperatures and this agrees well with our results found here for Ca II H and K and recent results for observations of the Ca II IR triplet (Marsden et al. 2009; Jackson & Jeffries 2010).

#### 5. CONCLUSIONS

Some extremely fast rotating stars show a decline in their coronal emission with increasing rotation. This effect has been termed *super-saturation* and as coronal X-rays cool down to chromospheric temperatures more cool loops emitting in chromospheric and transition region lines can exist but not in X-rays. We have investigated this idea by observing the Ca II H and K emission from a sample of rapidly rotating stars in both the northern and southern hemispheres. Our moderate resolution optical observations find a chromospheric saturation level of  $\log(L_{\text{CaK}}/L_{\text{bol}}) = -4.08$ . Comparison of  $L_{\text{CaK}}/L_{\text{bol}}$  with  $v \sin i$  shows no significant decrease for the fastest rotators. Similarly no decrease is observed for stars with  $\log(N_R) < -1.6$ . Our results are in agreement with recent studies of the Ca II IR triplet and thus no super-saturation exists in stellar chromospheres. However, as pointed out by many of these authors, the true causes of saturation and super-saturation are still an open topic.

This research made use of the Cerro Tololo Observatory, National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy, Inc. (AURA) under cooperative agreement with the National Science Foundation. The 2.5 m INT is operated on the island of La Palma by the Isaac Newton Group in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias. This work was also supported by the UK Science and Technologies Facilities Council (STFC). We thank Professor R. Jeffries for significantly improving the manuscript. D.C. acknowledges support from the CSUN College of Science. We also thank I. Skillen of ING NOAO for excellent support during our ING observations. This research has made use of the SIMBAD database, operated at CDS, Strasbourg, France.

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